through a 6-ft column of 25% Carbowax 20M on 60-80 Chromosorb W.

Mass Spectral Analysis. Mass spectral analysis of the isotopically labeled compounds was done with 70-V electrons with a Consolidated Model 21-103C spectrometer. Source and inlet temperatures were both 250°.

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# Weak Bases in Strong Acids. III.<sup>1</sup> Heats of Ionization of Amines in Fluorosulfuric and Sulfuric Acids. A New General Basicity Scale<sup>2</sup>

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Abstract: Some inherent difficulties in determining the  $pK_a$ 's of weak organic bases by acidity function methods are examined. The heat of protonation in an appropriate strong acid is proposed as an alternative criterion of base strength. As a test of this proposition, enthalpies of protonation for 35 amines, both aliphatic and aromatic, have been measured calorimetrically at 25° in pure fluorosulfuric acid and concentrated sulfuric acid. A good linear correlation between these enthalpies and the  $pK_a$  values of the corresponding conjugate acids in water is found spanning a range of 40 kcal/mole in enthalpy and 22  $pK_a$  units. The correlation coefficient is 0.992. The significance of enthalpy-free energy correlations is discussed. Such diverse types of compounds as primary, secondary, and tertiary aromatic and aliphatic amines, pyridines, cyclopropenones, nitroaromatics, phosphine oxides, and acid chlorides fit the  $\Delta H$ -p $K_a$  correlation and it is used to estimate the p $K_a$ 's (±0.7) of alcohols, ethers, water, and triphenylamine.

The transfer of protons from Bronsted acids to basic I molecules in solution is probably the most important and general reaction in chemistry.<sup>4</sup> All organic compounds are acids or bases (or both) and their ability to undergo proton transfer is an important criterion of their reactivity. Accurate measurements of proton transfer thermodynamics are, therefore, of fundamental chemical interest. They are also essential for the detailed kinetic interpretation of acid- and base-catalyzed reactions which, in turn, comprise the largest single class of reaction mechanisms in organic and biological chemistry.<sup>5</sup>

The aqueous pH scale is the traditional standard of reference for determination of  $pK_a$ 's of acid-base equilibria.<sup>6</sup> However, less than a half-dozen of the hundred-odd functional groups commonly encountered in organic chemistry ordinarily give measurable protolysis in the pH range of proton activity, although it has

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been known for years that most of them are completely protonated in concentrated sulfuric acid.<sup>7</sup> Hammett's suggestion<sup>8</sup> that the pH range be extended to strong aqueous sulfuric acid solutions through an indicatorbased acidity function was, therefore, a reasonable approach to the quantitative comparison of weak bases. Despite three decades of effort by many ingenious experimenters, the strengths of most classes of weak organic bases are poorly defined. The refined acidity function developed by Jorgenson and Hartter<sup>9</sup> for primary aniline indicators has not proven to be generally applicable to other families of bases in concentrated aqueous acid solutions. Its failure has been demonstrated for tertiary aromatic amines, 10 pyrroles, 11 indoles,<sup>12</sup> azulenes,<sup>13</sup> esters,<sup>14</sup> amides,<sup>15</sup> ketones,<sup>16</sup> alde-

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hydes,<sup>16b,d</sup> phosphine oxides,<sup>17</sup> pyridine 1-oxides,<sup>18</sup> phosphinates, 19 uraciles, 20 phloroglucinol and its methyl ethers,<sup>21</sup> sulfonamides,<sup>22</sup> carboxylic acids,<sup>16a,d,28</sup> thiohydantoins,<sup>24</sup> diarylolefins,<sup>25</sup> and arylmethanols.<sup>26</sup> Special acidity functions have been generated for some of these classes. The acidity function behavior of numerous other important classes of organic compounds has still not even been approached.

Since the Hammett indicator approach has failed to produce an acidity function which is applicable to all classes of weak bases in aqueous sulfuric acid, workers in the field have sought other solvent-acid combinations in which the activity coefficient postulate<sup>7g,27</sup> might be more generally valid. This has met with only limited success. Acidity function scales have been defined recently<sup>28</sup> for HCl-ethanol,<sup>29</sup> HBr-aqueous acetic acid,<sup>30</sup> H<sub>2</sub>SO<sub>4</sub>-aqueous ethanol,<sup>31</sup> H<sub>2</sub>SO<sub>4</sub>-aqueous 2-butoxyethanol,<sup>32</sup> HClO<sub>4</sub>-aqueous ethanol,<sup>33</sup> various acids in sulfolane, 34 and aqueous p-toluenesulfonic acid. 35

Another approach to the problem is that suggested by Bunnett and Olsen,<sup>36</sup> who have developed a linear free energy relationship to determine the thermodynamic  $pK_a$  of a base from indicator ratios by means of the equation

$$\log [BH^+]/[B] + H_0 = \phi(H_0 + \log [H^+]) + pK_{BH^+}$$

where  $\phi$  is the slope of the linear plot characterizing the response of the indicator ratio [BH+]/[B] to changing acid concentration. Yates<sup>14a</sup> has used an expression of similar form to estimate the  $pK_a$ 's of non-Hammett

$$\log [BH^+]/[B] = -mH_0 + pK_a$$

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bases and Johnson<sup>16b</sup> has shown that the two expressions give good agreement for carbonyl bases.

The failure of the Hammett activity coefficient assumption, with consequent proliferation of acidity functions specific to various classes of compounds, is now widely recognized. What is not realized so generally is the experimental difficulty of determining a reliable value for the indicator ratio referring unequivocally to a simple Brønsted equilibrium. Indeed, it may be said that although the  $pK_a$ 's of strong bases in weak acid are clearly defined by a variety of methods which agree well, the pK<sub>a</sub>'s of most weak bases in strong acids are badly defined operationally.

A major limitation on the determination of accurate indicator ratio values in aqueous sulfuric acid through absorption spectra is the problem of correcting for medium effects. These can cause variation in both the intensity and position of absorption bands as the acid concentration is varied, even though there is no evidence that the base is suffering protonation.<sup>16b</sup> This is not a serious problem for aniline indicators for which the disappearance of free base is followed by observing the decreasing intensity of the (  $n \rightarrow \pi^*$ ) band as the nonbonding electrons on nitrogen are coordinated with protons. For other types of spectral transitions the problem can be serious. Several methods of interpretation have been developed to correct for these medium effects; however, the calculated  $pK_a$  values are sensitive to the correction technique employed and the choice between them is often rather subjective.

A case in point is the wide disagreement between many groups on the best treatment of absorption spectra for conjugated aldehydes and ketones in strong aqueous acid of varying strength.<sup>16b,d</sup>

Not all of the problems encountered in determining the strengths of weak bases can be ascribed to the limitations of the Hammett acidity function or to the difficulties of correcting for medium effects in the region of protonation. For many important types of compounds, the region of protonation cannot even be defined operationally with consistency. Different analytical methods lead to different indicator ratios at a given acid concentration, and thus, different  $pK_a$ 's at the standard state of dilute aqueous acid. Table I contains a summary of available  $pK_a$  values for some important compounds and the methods used in their determination. Their failure to agree does not necessarily reflect any lack of ingenuity or care on the part of the experimenters whose conflicting values are juxtaposed. Rather, it reflects the uncertainties of interpreting apparent solute concentration variations as the acidity changes.

The range of these  $pK_a$  estimates obtained with a variety of probes suggests that processes other than complete proton transfer are affecting the results. A number of authors<sup>7g,87</sup> have suggested that these effects are due to varying degrees of solvent-solute interaction (e.g., hydrogen bonding) as a function of acid concentration. These results were anticipated by the early solubility work of Hammett, 38 which showed drastic

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Table I. Literature Values for  $pK_a$ 's of Several Weak Bases

Compound	pK <sub>a</sub>	Analytical method		
Acetone	-0.24	Calorimetric <sup>a</sup>		
	-0.3	Electrical conductivity <sup>b</sup>		
	-0.46	Competitive indicator (uv) <sup>c</sup>		
	-1.6	Indicator $(uv)^d$		
	-3.0	Solvent extraction <sup>e, f</sup>		
	<-4.5	Competitive indicator (uv) <sup>o</sup>		
	-7.2	Indicator (uv) <sup>h</sup>		
	-7.2	Raman <sup>i</sup>		
	-7.2	Nmr <sup>i</sup>		
Diethyl ether	-0.30	Competitive indicator (uv) <sup>i</sup>		
-	-0.47	Electrical conductivity <sup>k</sup>		
	-3.53	Vapor pressure <sup>1</sup>		
	<b>— 3 . 59</b>	Solvent extraction <sup>m</sup>		
	-4.14	Solvent extraction <sup>e</sup>		
	-5.7	Titration <sup>n</sup>		
	-6.2	Nmr°		
Ethanol	-0.33	Calorimetric <sup>a</sup>		
	-0.33	Electrical conductivity <sup>p</sup>		
	-2.3	Kinetics <sup>q</sup>		
	-4.8	Nmr <sup>o</sup>		
Methanol	-0.34	Electrical conductivity <sup>p</sup>		
	-1.05	Competitive indicator (uv) <sup>7</sup>		
	-2.2	Raman <sup>i</sup>		
	-4.9	Raman <sup>®</sup>		
2-Propanol	-0.35	Electrical conductivity <sup>p</sup>		
•	-0.47	Competitive indicator (uv) <sup>7</sup>		
	-2.5	Solvent extraction <sup>q,f</sup>		
	-3.2	Kinetics <sup><i>t</i></sup>		
	-3.8	Kinetics <sup>u</sup>		
	<-4.5	Kinetics <sup>v</sup>		
	-4.7	Raman*		
	-5.2	Raman <sup>*</sup>		

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acidity dependence for the solubilities of nitrobenzene and benzoic acid in a series of aqueous sulfuric acid media which were too weak to give any measurable degree of protonation of these bases.

We believe that the ambiguity associated with free energy measurements of weak bases in continually changing strong acid media is a fundamental problem which will only be more exhaustively documented rather than "solved" by further use of the acidity function approach. This belief has stimulated us to seek other criteria for discussing base strengths.

Heats of interaction have been measured for many strong bases with strong protonic<sup>39</sup> and Lewis acids.<sup>40</sup> The complexing of a number of weak bases with Lewis acids has also been measured calorimetrically.<sup>41</sup> However, this technique has not been systematically applied to the study of weak bases with strong protonic acids. the field of our present inquiry. This paper and the one following it in this series report such an investigation and the establishment through it of an independent basicity scale based on enthalpies of protonation for most types of weak bases in a single acid medium, fluorosulfuric acid. For comparison, some results for concentrated sulfuric acid are also presented.

### **Experimental Section**

Chemicals. Most of the compounds used in this study were available commercially. Liquids were generally dried, using an appropriate agent, and then distilled. Solids were recrystallized and dried. Some were purified by vacuum sublimation. All melting points, boiling points, and refractive indices were in good agreement with literature values. Carbon tetrachloride (Baker reagent grade) was stored over Linde Type 4A molecular sieves. sym-Tetrachlorethane (Eastman White Label) was passed through a column of neutral alumina before use. Concentrated sulfuric acid (Baker and Adamson C. P. grade) was used as received. Fluorosulfuric acid (Baker and Adamson Technical Grade) was flushed with dry nitrogen and distilled, bp 163°. Further details regarding the purification and physical constants of many of the compounds investigated may be found in the Ph.D. thesis of J. J. Burke.

Calorimetric Methods. The calorimetric equipment and procedures are basically as described previously.42 Stainless steelcoated, 2090-ohm thermistors (Keystone Carbon Co., St. Marys, Pa.) were used in fluorosulfuric acid. All of the heat measurements were calibrated electrically. Solid samples were introduced into fluorosulfuric acid (contained in a 200-ml dewar flask) by means of a modified plastic 1-cc syringe (Pharmaseal Laboratories, Glendale, Calif.) with a Teflon tape-covered plunger and a solid Teflon plug to protect the sample from the acid solution during thermal equilibration. Liquid samples were introduced by means of Hamilton syringes (509  $\mu$ l, gas tight with Chaney adapter) using calibrated stainless steel stops to deliver accurately and reproducibly ca. 100  $\mu$ l of solute. Sample sizes ranged from 50 to 150  $\pm$  0.2 mg, depending on the magnitude of the observed heats so as to give optimum displacement of the recorder pen.

## Results

Systematic errors were detected and avoided by frequent checks of the calorimeters against well-accepted values for the heats of solution of solutes in the systems under investigation. The accuracy and precision of our calorimetric methods can be evaluated by comparison of our data with literature values as listed in Table II. The error limits represent standard deviations mostly from the mean of seven dependent measurements. Incidentally, these results and many others gathered in this laboratory over the past 5 years attest to the accuracy as well as convenience of our unorthodox procedure of introducing samples via syringes in-

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Table II. Comparison of Observed Heats of Solution with Literature Values for Various Solutes and Solvents

Solute	Solvent	$-\Delta \vec{H}_{obsd}$ at 25°, kcal/mole	$-\Delta \vec{H}_{ m lit.}$ at 25°, kcal/mole		
KCla	H <sub>2</sub> O	$-4.10 \pm 0.06$	$-4.115 \pm 0.01^{b}$		
		$-4.12 \pm 0.05$ $-4.15 \pm 0.03$			
		$-4.11 \pm 0.06$			
NH₄Cl	$H_2O$	$-0.94 \pm 0.01$	$-0.975 \pm 0.025^{b}$		
Pyridine	H₂O	$2.28 \pm 0.08$	$2.32 \pm 0.010^{\circ}$		
Ethanol	H <sub>2</sub> O	$2.43 \pm 0.04$	$2.39 \pm 0.02^{d}$		
H <sub>2</sub> O	39.94% H₂SO₄	$0.336 \pm 0.012$	0.348*		
$H_2O$	50.09% H <sub>2</sub> SO <sub>4</sub>	$0.672 \pm 0.009$	0.666°		
H <sub>2</sub> O	59.54% H₂SO₄	$1.113 \pm 0.021$	1.098*		
$H_2O$	69.63% H <sub>2</sub> SO <sub>4</sub>	$1.870 \pm 0.029$	1.866*		
H₂O	80.53% H₂SO₄	$3.591 \pm 0.045$	3.574*		
H <sub>2</sub> O	89.73 % H₂SO₄	$6.307 \pm 0.043$	6.360°		
Nitrobenzene	FSO <sub>3</sub> H	$5.63 \pm 0.09$	$5.55 \pm 0.2^{f}$		
Benzoic acid	FSO₃H	$6.20 \pm 0.2$	$8.80 \pm 0.25'$		
$H_2O$	FSO₃H	$12.2 \pm 0.1$	$11.95 \pm 0.04'$		
Acetic acid	FSO₃H	$13.1 \pm 0.2$	$13.26 \pm 0.1'$		

<sup>a</sup> Four different calorimeters were used during the course of this investigation. <sup>b</sup> V. B. Parker, "Thermal Properties of Aqueous Uniunivalent Electrolytes," National Standard Reference Data Series, National Bureau of Standards, 2, Washington, D. C., 1965. C. Sacconi, P. Paoletti, and M. Ciampolina, J. Am. Chem. Soc., 82, 3828 (1960). <sup>d</sup> R. Aveyard and A. S. C. Lawrence, Trans. Faraday Soc., 60, 2265 (1964). <sup>e</sup> W. F. Giauque, E. W. Hornung, J. E. Kunzler, and T. R. Rubin, J. Am. Chem. Soc., 82, 62 (1960). <sup>f</sup> G. W. Richards and A. A. Woolf, J. Chem. Soc., A, 470 (1968).

stead of the conventional technique of breaking glass ampoules.

The agreement of our results with literature values is excellent except for the heat of solution of benzoic acid in fluorosulfuric acid. We have made several measurements with samples of benzoic acid which had been recrystallized, sublimed, or zone refined and have still failed to obtain argeement with Woolf's value. We are unable to explain the discrepancy.

The heats of solution at 25° in carbon tetrachloride, sym-tetrachloroethane, 96.48% sulfuric acid, and fluorosulfuric acid are listed in Table III. The heats of protonation of several oxygen bases are listed in Table IV using both the gas phase and carbon tetrachloride as standard states. Of necessity heats of solution at infinite dilution in these inert solvents (sym-tetrachloroethane or carbon tetrachloride) rather than the gas phase have been used to correct the heats of solution in acids for the energy associated with separating the solute molecules. This procedure has been justified previously by the observation that the relative differences in heats of formation of carbonium ions were the same using either the gas phase or dilute carbon tetrachloride solutions as the reference state for the unprotonated precursor.43,44 Furthermore, the heats of solution of approximately 100 unassociated liquid solutes measured here<sup>45</sup> in carbon tetrachloride are in the range 0.0  $\pm$ 1.0 kcal/mole, indicating (by this criterion) the usual formation of nearly perfect solutions in this medium. sym-Tetrachloroethane was used as a reference solvent for several nitroaniline bases because they were insoluble in carbon tetrachloride. We have avoided its use whenever possible, however, because of its potential ability as a C-H hydrogen bond donor to basic solutes

(43) E. M. Arnett and J. W. Larsen, J. Am. Chem. Soc., 91, 1438 (1969). (44) For comparison of adduct formation in the gas phase and in solution see (a) L. J. Sacks, R. S. Drago, and D. P. Eyman, Inorg. Chem., 7, 1484 (1968); (b) W. Partenheimer, T. D. Epley, and R. S. Drago, J. Am. Chem. Soc., 90, 3886 (1968); (c) J. M. Goodenow and M. Tamres, J. Chem. Phys., 43, 3393 (1965); (d) F. T. Lang and R. L. Strong, J. Am. Chem. Soc., 87, 2345 (1965).

45) Unpublished data of J. V. Carter, E. Mitchell, T.S.S.R. Murty, J. W. Larsen, and R. P. Quirk in this laboratory.

with consequent errors from the enthalpy of hydrogen bonding. 46

#### Discussion

Basicity Scales. We propose the enthalpies of protonation listed in Table III as a useful criterion of base strength. The responsiveness of this property to structural variations is demonstrated through comparison of the heats of protonation of triethylamine (-49.1)kcal/mole) and trinitroaniline (-13.2 kcal/mole) in FSO<sub>3</sub>H while the heat of solution of a typical nonbase, carbon tetrachloride, in FSO<sub>3</sub>H is (+) (sic.) 1.8 kcal/ mole. In Figure 1 our calorimetrically determined heats of protonation are plotted vs. the corresponding

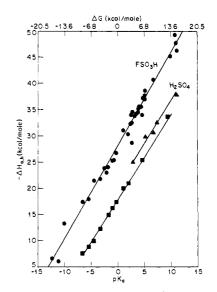


Figure 1. Heats of protonation of amines in strong acids vs.  $pK_{s}$ values of their conjugate acids in water:  $\bullet$ , amines in FSO<sub>3</sub>H;  $\blacktriangle$ , pyridines and piperidine in 96.48 % H₂SO₄; ■, anilines and benzylamine in 96.48% H<sub>2</sub>SO<sub>4</sub>.

<sup>(46)</sup> A. Allerhand and P. von R. Schleyer, J. Am. Chem. Soc., 85, 1715 (1963).

Table III.	Thermodynamic Quantities for the Protonation of Bases in FSO <sub>3</sub> H and 96.4% H <sub>2</sub> SO <sub>4</sub> at 25° from CCl <sub>4</sub> or	
sym-Tetrac	hloroethane Reference State	

Compound	$-\Delta H_{ m FSO_3H}{}^a$	$-\Delta H_{\mathrm{H_{2}SO_{4}}^{b}}$	$-\Delta H_{\rm CC14}^{c}$	$-\Delta H_{sym}{}^d$	$\Delta H_{\mathrm{a,b}}$	$\Delta H_{\rm a,b}$	pK <sub>a</sub>
Triethylamine	$49.8 \pm 0.03$		$+0.64 \pm 0.08$		$49.2 \pm 0.3$		10.75 <sup>h</sup>
Diethylamine	$48.1 \pm 0.3$		$+0.42 \pm 0.06$		$47.7 \pm 0.3$		10.98 <sup>h</sup>
Piperidine		$39.9 \pm 0.3$		$2.08 \pm 0.06$		$37.8 \pm 0.4$	$11.12^{h}$
Di- <i>n</i> -butylamine	$46.7 \pm 0.5$		$+0.3 \pm 0.05$		$46.4 \pm 0.5$		11.25
Tri- <i>n</i> -butylamine	$45.0 \pm 0.3$		$-0.21 \pm 0.08$		45.2 + 0.3		9.93 <sup></sup>
Benzylamine		$35.5 \pm 0.6$		$1.82 \pm 0.01$		$33.7~\pm~0.6$	9.35 <sup>h</sup>
2,4,6-Trimethylpyridine		$35.2 \pm 0.5$		$2.61 \pm 0.01$		$32.6~\pm~0.5$	7.43 <sup>h</sup>
2,6-Lutidine	$41.0 \pm 0.2$	$32.9 \pm 0.4$	$+0.27 \pm 0.08$	$2.27 \pm 0.08$	$41.3 \pm 0.2$	$30.6~\pm~0.5$	6.72 <sup>h</sup>
Pyridine	$38.2 \pm 0.2$	$31.7 \pm 0.3$	$-0.36 \pm 0.02$	$1.84 \pm 0.01$	$38.6 \pm 0.2$	$29.9 \pm 0.3$	5.21
N,N-Dimethylaniline	$37.6 \pm 0.3$		$-0.12 \pm 0.01$		$37.7 \pm 0.3$		5.07*
4-Fluoroaniline	$35.1 \pm 0.09$		$-2.09 \pm 0.04$		$37.2 \pm 0.1$		4.65 <sup>h</sup>
4-Methylaniline	$31.4 \pm 0.3$		$-5.54 \pm 0.05$		$36.9 \pm 0.3$		5.08 <sup>h</sup>
4-Chloroaniline	$28.9 \pm 0.4$		$-6.73 \pm 0.09$		$35.6 \pm 0.4$		3.98 <sup>h</sup>
2-Methylaniline	$34.0 \pm 0.2$		$-1.59 \pm 0.05$		35.6 + 0.2		4.45 <sup>h</sup>
4-Bromoaniline	$29.3 \pm 0.4$		$-5.88 \pm 0.02$		$35.2 \pm 0.4$		3.86 <sup>h</sup>
3-Bromopyridine	$34.4 \pm 0.4$	$26.3 \pm 0.2$	$-0.23~\pm~0.03$	$1.32 \pm 0.07$	$34.6~\pm~0.4$	$25.0~\pm~0.3$	$2.84^{h}$
4-Iodoaniline	$28.0 \pm 0.5$		$-6.5 \pm 0.2$		$34.5~\pm~0.5$		3.78 <sup>ħ</sup>
3-Chloroaniline	$32.2 \pm 0.2$		$-2.02 \pm 0.04$		$34.2 \pm 0.2$		3.52 <sup>h</sup>
3-Nitroaniline	$29.0 \pm 0.3$			$-5.0 \pm 0.1$	$34.0 \pm 0.3$		2.47 <sup>h</sup>
Aniline	$34.3 \pm 0.4$	25.8		$0.31~\pm~0.02$		$25.5~\pm~0.2$	4.60 <sup>h</sup>
2-Fluoroaniline	$32.2 \pm 0.1$		$-1.72 \pm 0.02$		$33.9 \pm 0.1$		3.20 <sup>h</sup>
2-Chloroaniline	$30.5 \pm 0.2$		2.0		$32.5~\pm~0.2$		2.65 <sup>h</sup>
4-Nitroaniline	$27.0 \pm 0.3^{g}$	$15.9 \pm 0.2$		$-4.14 \pm 0.04$		$20.0~\pm~0.2$	$1.00^{h}$
2-Iodoaniline	$26.0 \pm 0.1$		$-6.4 \pm 0.2$		$32.4 \pm 0.2$		2.55 <sup>h</sup>
2,4-Dichloroaniline	$24.1 \pm 0.2$	$15.9 \pm 0.5$	$-6.2 \pm 0.1$	$-5.06 \pm 0.06$		$21.0~\pm~0.6$	$2.00^{h}$
Triphenylphosphine <sup>p</sup>	$24.9 \pm 0.3$		$-3.83 \pm 0.1$		$28.7~\pm~0.3$		2.731
2-Nitroaniline	$22.8~\pm~0.3$	$13.4 \pm 0.2$		$-3.99 \pm 0.02$	$26.8 \pm 0.3$	$17.4 \pm 0.2$	-0.26 <sup>h</sup>
2,4,6-Tribromoaniline	$18.5 \pm 0.4$		$-6.8 \pm 0.3$		$25.3 \pm 0.5$		0.81
4-Chloro-2-nitroaniline	$20.9 \pm 0.5$	$11.8 \pm 0.2$		$-4.40 \pm 0.05$	$25.3~\pm~0.5$	$16.2 \pm 0.3$	$-1.02^{h}$
2,5-Dichloro-4-nitroaniline	$19.0~\pm~0.2$	$9.8 \pm 0.3$		$-5.11 \pm 0.16$		$14.9~\pm~0.5$	$-1.78^{k}$
Diphenylcyclopropenone	$18.7 \pm 0.3$		$-5.2 \pm 0.2$		$23.9 \pm 0.4$		$-2.5^{i}$
Triphenylphosphine oxide	$18.8 \pm 0.2$		$-4.2 \pm 0.2$		$23.0~\pm~0.3$		$-2.10^{m}$
Benzene	$18.6 \pm 0.3$	_				_	
2,6-Dichloro-4-nitroaniline		$6.8 \pm 0.7$		$-5.41 \pm 0.01$	$21.8 \pm 0.2$	$12.2 \pm 0.7$	$-3.27^{k}$
2,4-Dinitroaniline	$17.2 \pm 0.2$	$5.6 \pm 0.9$		$-4.29 \pm 0.07$	$21.5~\pm~0.2$	$9.9 \pm 1.0$	$-4.53^{h}$
Triphenylamine	$15.3 \pm 0.5$		$-3.8 \pm 0.1$		$19.1 \pm 0.5$		
2,6-Dinitroaniline	$14.5 \pm 0.2$	$5.4 \pm 0.2$		$-3.43 \pm 0.04$		$8.8 \pm 0.2$	- 5.54 <sup>k</sup>
2-Bromo-4,6-dinitroaniline	$13.1 \pm 0.3$	$3.2 \pm 0.4$		$-4.27 \pm 0.01$	$17.4 \pm 0.3$	$7.5 \pm 0.4$	$-6.68^{k}$
2,4,6-Trinitroaniline	$9.0~\pm~0.2$	$-1.2 \pm 0.2$		$-4.17 \pm 0.15$	$13.2 \pm 0.3$		$-10.1^{k}$
Nitrobenzene	$5.63 \pm 0.09$		$-1.25 \pm 0.02$	$-1.0 \pm 0.01$	$6.6 \pm 0.1$		$-12.42^{n}$
Benzoyl chloride	$5.3 \pm 0.5$		$-0.7 \pm 0.1$		$6.0 \pm 0.5$		-11.150
Carbon tetrachloride	$+1.79 \pm 0.06$						

<sup>a</sup> Heat of solution of pure compound into FSO<sub>3</sub>H in kcal/mole. <sup>b</sup> Heat of solution of pure compound into 96.48% H<sub>2</sub>SO<sub>4</sub> in kcal/mole. <sup>c</sup> Heat of solution of pure compound into CCl<sub>4</sub> in kcal/mole. <sup>d</sup> Heat of solution of pure compound into *sym*-tetrachloroethane in kcal/mole. <sup>e</sup> Heat of transfer of pure compound from the inert solvent to FSO<sub>3</sub>H in kcal/mole. <sup>f</sup> Heat of transfer of pure compound from inert solvent to 96.48% H<sub>2</sub>SO<sub>4</sub> in kcal/mole. <sup>e</sup> A value of -28.0 ± 0.3 kcal/mole was obtained at 10 ± 2°. <sup>h</sup> See ref 61. <sup>i</sup> W. A. Henderson and C. A. Streuli, *J. Am. Chem. Soc.*, 82, 5791 (1960). <sup>i</sup> E. Sawicki and F. E. Ray, *J. Org. Chem.*, 19, 1686 (1954). <sup>k</sup> See ref 9. <sup>i</sup> R. Breslow, T. Eicher, A. Krebs, R. A. Peterson, and J. Posner, *J. Am. Chem. Soc.*, 87, 1320 (1965). <sup>m</sup> C. Klofutar, F. Krasovec, and M. Kusar, *Croat. Chem. Acta*, 40, 23 (1968). <sup>n</sup> See ref 51. <sup>o</sup> M. Liler, *J. Chem. Soc.*, 8, 205 (1966). <sup>p</sup> Unpublished results of E. Mitchell.

Table IV. Heats of Protonation of Several Oxygen Bases

Compound	$\Delta H_{\rm FSO_{3H}},$ kcal/mole	$\Delta H_{\rm CCl_4},$ kcal/mole	$\Delta H_{vap},$ kcal/mole	$\Delta H_{i,a}$ kcal/mole	$\Delta H_{a,b}$ , bkcal/mole
Tetrahydrofuran	$-20.2 \pm 0.2$	$-0.60 \pm 0.02$	7.6°	-27.8	- 19.6
Diethyl ether	$-19.5 \pm 0.7$	$-0.42 \pm 0.01$	6.5ª	-26.0	-19.1
Ethanol	$-15.3 \pm 0.3$	3.8	10.3 <sup>d</sup>	-25.6	- 19.1
Acetone	$-18.3 \pm 0.1$	$0.79 \pm 0.02$	7.1ª	-25.4	- 19.1
Water	$-12.2 \pm 0.1$	4.2°	10.5 <sup>d</sup>	-22.7	-16.4

<sup>a</sup> Heat of transfer from the gas phase to FSO<sub>3</sub>H. <sup>b</sup> Heat of transfer from CCl<sub>4</sub> to FSO<sub>3</sub>H. <sup>c</sup> B. Watson, Ph.D. Thesis, University of Bradford, 1968. <sup>d</sup> A. Weissberger, "Technique of Organic Chemistry," Vol. VII, Interscience Publishers, New York, N. Y., 1955. <sup>e</sup> Heat of solution of H<sub>2</sub>O into *sym*-tetrachlooroethane. Unpublished work of Dr. J. V. Carter.

 $pK_a$  values.<sup>47</sup> The reader should note that a good linear correlation between these two basicity properties holds over the enormous range of 40 kcal/mole for the enthalpies and 22  $pK_a$  units (28 kcal/mole in

free energy) from the weakly basic benzoyl chloride and nitrobenzene to the strongly basic alkylamines. Least squares equations for these data are as follows.

(47) The standard state for the heats of protonation is either dilute CCl<sub>4</sub> or *sym*-tetrachloroethane. The standard state for the  $pK_a$ 's is dilute aqueous solution.

 $-\Delta \bar{H}$  (anilines, 96.48% H<sub>2</sub>SO<sub>4</sub>) =

 $(1.62 \text{ p}K_{a} + 17.9) \text{ kcal/mole} (1)$ 

 $-\Delta \bar{H}$  (pyridines, 96.48% H<sub>2</sub>SO<sub>4</sub>) = (1.65 pK<sub>a</sub> + 20.3) kcal/mole (2)

$$-\Delta \vec{H}$$
 (amines, FSO<sub>3</sub>H) =

$$(1.78 \text{ p}K_a + 28.1) \text{ kcal/mole}$$
 (3)

The standard deviations of the slope and intercept for eq 3 were 0.04 and 0.22, respectively. The average deviation of points from the correlation line was 1.2 kcal/mole and the correlation coefficient was 0.992. Consideration of these errors leads us to set error limits of  $\pm 0.7$  on pK<sub>a</sub>'s predicted from this correlation. The correlation of our heats of protonation with the best available (see below) estimates of pK<sub>a</sub>'s in dilute aqueous solutions provides justification for the use of these heats as an independent measure of basicity.

This enthalpimetric basicity scale provides a useful tool for examining the effects of small structural changes on basicity because of the expanded scale resulting from the use of very strong acids (see the slopes and intercepts of eq 1, 2, and 3).

The use of FSO<sub>3</sub>H, however, limits the range of substituents to groups which will not themselves interact strongly with the acid. Thus, benzene gave a very high apparent heat of solution ( $-18.6 \pm 0.3$  kcal/mole) in FSO<sub>3</sub>H (probably because of rapid exothermic sulfonation<sup>45</sup>). This warns us of a possible source of error in the study of other aromatic bases.

Different families of bases apparently generate their own  $\Delta H - \Delta G^{\circ}$  correlations in H<sub>2</sub>SO<sub>4</sub>, while no such resolution into families could be detected in fluorosulfuric acid. Such diverse classes of bases as primary, secondary, and tertiary aromatic and aliphatic amines, pyridines, nitroaromatics, cyclopropenones, acid chlorides, phosphines, and phosphine oxides are displayed for the  $\Delta H - \Delta G^{\circ}$  correlation in fluorosulfuric acid.

In addition to generating a larger range of enthalpy values, fluorosulfuric acid possesses several other characteristics which make it preferable to sulfuric acid. Fluorosulfuric acid has a much lower viscosity (1.5649 vs. 24.5 cP for  $H_2SO_4^{7d}$  and higher dielectric constant (ca.  $120^{50}$  vs. 100 units for H<sub>2</sub>SO<sub>4</sub><sup>7d</sup>) than concentrated sulfuric acid. Serious solubility and mixing problems were encountered in attempting to extend our  $\Delta H - \Delta G^0$  scale in  $H_2SO_4$  to aromatic carbonyl compounds, but we have never encountered any solubility problems or solute concentration dependence in fluorosulfuric acid. A further advantage of fluorosulfuric acid is its greater acidity, which probably accounts for larger heats measured in it. Gillespie and coworkers have assigned an  $H_0$  acidity function value of -13.9 to FSO<sub>3</sub>H compound with -12.1 for 100% H<sub>2</sub>SO<sub>4</sub>.<sup>49</sup> Thus, nitrobenzene (p $K_a - 12.4^{51}$ ), which is incompletely protonated in 99.5% H<sub>2</sub>SO<sub>4</sub>, is completely ionized within the limits of measurement in FSO<sub>3</sub>H.<sup>50</sup>

The use of enthalpies of protonation as a measure of basicity possesses several distinct advantages over the free energy measurements obtained by acidity function techniques. The former are carried out in a single medium and so are free of ambiguous medium effects found in studying protonation equilibria. Furthermore, the

(48) J. W. Simons, H. J. Passino, and S. Archer, J. Am. Chem. Soc., 63, 608 (1941).

(49) R. J. Gillespie, Accounts Chem. Res, 1, 202 (1968).

(50) J. Barr, R. J. Gillespie, and R. C. Thompson, Inorg. Chem., 3, 1149 (1964).

(51) K. Yates and A. A. Thompson, Can. J. Chem., 45, 2997 (1967).

calorimeter. It was not anticipated that the heats of protonation for aniline bases in FSO<sub>3</sub>H or concentrated H<sub>2</sub>SO<sub>4</sub> would correlate with aqueous  $pK_a$  values. Many of these were determined by the Hammett overlap procedure<sup>5d,7g</sup> which relies on a lengthy extrapolation to the standard state of infinite dilution in water. Previous justification for this overlap procedure was based on (a) the approximate parallelism of log [BH<sup>+</sup>]/[B] vs. [H<sup>+</sup>] plots and (b) the constant  $\Delta pK_a$  values for two indicators in different solvents. The correlation of  $pK_a$ values determined by this procedure with heats of protonation in strong acids is a third justification for the overlap method of estimating  $pK_a$  values.

troscopy.<sup>7d,49,50,52</sup> Finally, our heat measurements are

accurately and relatively easily obtained using a simple

 $\Delta H^{\circ} - \Delta G^{\circ}$  Correlations. Although the question of whether enthalpy or free energy is a better measure of potential energy is debatable, most chemists prefer free energy measurements as a practical expression of chemical driving force. Enthalpy measurements can be expected to parallel free energy changes in another medium in those cases where linear free energy correlations<sup>7b,53</sup> and isokinetic or isoentropic relationships<sup>7b,53a</sup>, e<sub>1</sub>, st simultaneously. This can be demonstrated readily as follows.

Using the operator formalism of Leffler and Grunwald,<sup>53d</sup> the effect of a substituent change, R, on the basic thermodynamic quantities can be expressed as

$$\delta_{\rm R} \Delta G_{\rm w}^{\,\circ} = \,\delta_{\rm R} \Delta H_{\rm w}^{\,\circ} - \,T \delta_{\rm R} \Delta S_{\rm w}^{\,\circ} \tag{4}$$

in water and

$$\delta_{\rm R} \Delta G_{\rm a}^{\,\circ} = \,\delta_{\rm R} \Delta H_{\rm a}^{\,\circ} - \,T \delta_{\rm R} \Delta S_{\rm a}^{\,\circ} \tag{5}$$

in acid. If an isokinetic relationship exists in the acid solution, then

 $\delta_{\rm R} \Delta H_{\rm a}^{\,\circ} = \beta \delta_{\rm R} \Delta S_{\rm a}^{\,\circ}$ 

and

$$\delta_{\rm R} \Delta G_{\rm a}^{\circ} = \delta_{\rm R} \Delta H_{\rm a}^{\circ} [1 - (T/\beta)]$$

If the effects of molecular structure variation on free energies in the two media are also proportional so that

$$\delta_{\rm R} \Delta G_{\rm w}^{\,\circ} = \rho_{\rm M} \delta_{\rm R} \Delta G_{\rm a}^{\,\circ} \tag{8}$$

(6)

then by combination of eq 7 and 8, it follows that

$$\delta_{\rm R} \Delta G_{\rm w}^{\,\circ} = \rho_{\rm M} \delta_{\rm R} \Delta H_{\rm a}^{\,\circ} [1 - (T/\beta)] \tag{9}$$

where  $\delta_{R}$  represents the substituent operator and  $\beta$  and  $\rho_{m}$  are isokinetic and linear free energy proportionality constants, respectively.

(52) (a) T. Birchall, A. N. Bourns, R. J. Gillespie, and P. J. Smith, Can. J. Chem., 42, 1433 (1964); (b) R. J. Gillespie, J. B. Milne, and R. C. Thompson, *Inorg. Chem.*, 5, 468 (1966); (c) T. Birchall, Ph.D. Thesis, McMaster University, 1963; (d) R. J. Gillespie and T. Birchall, Can. J. Chem., 41, 148 (1963).

Can. J. Chem., 41, 148 (1963).
(53) (a) C. D. Ritchie and W. F. Sager, Progr. Phys. Org. Chem., 2, 323 (1964); (b) P. R. Wells, Chem. Rev., 63, 171 (1963); (c) H. H. Jaffé, Chem. Rev., 53, 191 (1953); (d) J. E. Leffler and E. Grunwald, "Rates and Equilibria in Organic Reactions," John Wiley & Sons, Inc., New York, N. Y., 1963.

(54) (a) J. E. Leffler, J. Org. Chem., 31, 533 (1966); (b) *ibid.*, 20, 1202 (1955); (c) M. G. Evans and M. Polanyi, *Trans. Faraday Soc.*, 32, 1333 (1936).

Linear  $\Delta H^{\circ} - \Delta G^{\circ}$  correlations would also be expected for an isoentropic series. Thus, if the entropy in acid solution were constant

$$\delta_{\rm R} \Delta S_{\rm a}^{\circ} = 0 \tag{10}$$

and thus from eq 5

$$\delta_{\rm R} \Delta G_{\rm a}^{\,\circ} = \,\delta_{\rm R} \Delta H_{\rm a}^{\,\circ} \tag{11}$$

The combination of eq 8 and 11 leads again to a relationship between  $\Delta G_{\mathbf{w}}^{\circ}$  and  $\Delta H_{\mathbf{a}}^{\circ}$ , *i.e.* 

$$\delta_{\rm R} \Delta G_{\rm w}^{\,\circ} = \rho_{\rm m} \delta_{\rm R} \Delta H_{\rm a}^{\,\circ} \tag{12}$$

Equations 6, 8, and 10 are extrathermodynamic relationships in the sense that they are not demanded by the formal structure of thermodynamics, although they are frequently observed as empirical correlations.<sup>53d</sup> The applicability of enthalpy-free energy correlations should be as general and as valid as linear free energy, isokinetic, or isoentropic ones since they may be derived from them.

Simple electrostatic theory for isoelectric reactions also predicts a linear relationship between  $\Delta H^{\circ}$  in acid solution and  $\Delta G^{\circ}$  in water.<sup>55a</sup> However, the multiplicity of terms involved in considering these equilibria<sup>55b</sup> precluded quantitative evaluation of this treatment.

Many of the isokinetic correlations reported so far cannot be accepted as heuristically significant. When both  $\Delta H^{\circ}$  and  $\Delta S^{\circ}$  are derived from the same experimental data through temperature coefficients of equilibrium or rate constants, errors in  $\Delta H^{\circ}$  are accompanied by corresponding errors in  $\Delta S^{\circ}$ . This can lead to a linear relationship between the errors in these quantities.54a,56 Less questionable  $\Delta H^{\circ} - \Delta S^{\circ}$  correlations are obtained using calorimetric enthalpies.<sup>57</sup> These do not include the first derivative errors common to van't Hoff-Arrhenius treatments. After critical examination of this field, Ritchie<sup>53a</sup> has concluded that good linear free energy and isokinetic correlations are rarely found simultaneously.<sup>58</sup> Within this framework, it is reasonable to look for  $\Delta H^{\circ} - \Delta G^{\circ}$  correlations in cases where reliable calorimetric enthalpies and free energies may be compared and use them to estimate structural effects on free energy in systems where  $\Delta G^{\circ}$  cannot be measured directly, as in FSO<sub>3</sub>H. We have previously reported examples of good linear  $\Delta H^{\circ} - \Delta G^{\circ}$  correlations for the calorimetric heats of protonation of polyalkylbenzenes in  $SbF_5$ -FSO<sub>3</sub>H vs. their free energies of protonation in HF<sup>59a</sup> and also for the calorimetric heats of ionization of triarylcarbinols in 96 % H<sub>2</sub>SO<sub>4</sub> vs. their free energies of ionization in dilute aqueous acid.59b

Although our correlations appear to be general, we anticipate that these  $\Delta H^{\circ} - \Delta G^{\circ}$  correlations will ultimately suffer from the same shortcomings as linear free energy correlations. The failure of the simple Ham-

mett  $\sigma \rho$  treatment to fit all cases of substituent effects on free energy change has led to a bewildering array of substituent "constants" in order to cover so-called anomalous situations.<sup>53a,b</sup> Medium effects on  $\Delta H^{\circ} - \Delta G^{\circ}$  correlations will probably fare even worse than linear free energy correlations of solvent effects such as the Hammett acidity function<sup>7b,g</sup> and the Winstein-Grunwald equation.<sup>60</sup> These are well known to be poorer correlations than those for structural change.

 $\mathbf{p}K_{\mathbf{a}}$  Estimates. The  $\Delta H^{\circ} - \Delta G^{\circ}$  correlation in Figure 1 and eq 3 can be applied to the estimation of base strengths of classes of compounds whose basicities are controversial or which cannot be studied in aqueous sulfuric acid. For example, by using eq 3 and the observed heat of protonation of triphenylamine, a  $pK_a$  value of -5.0 can be estimated for this compound referred to dilute aqueous solution. No previous estimate of its basicity is known to us, presumably because of its limited solubility in conventional acid solutions. This estimate for triphenylamine appears reasonable in view of the effect of phenyl groups on amine basicities ( $pK_a$ 's) in the series NH<sub>3</sub> (9.24) aniline (4.60), and diphenylamine (0.79).<sup>61</sup>

Our correlation also provides information about the relative basicities of alcohols, ethers, and water. The heats of protonation of several of these compounds are listed in Table IV. The gas phase and sym-tetrachloroethane have been chosen as the reference state for water because of its low solubility in CCl<sub>4</sub>. By our criterion of basicity, these compounds fall in the order ROR > $ROH \gg H_2O$ ; the same order was found by Munson for the gas phase proton affinities of these compounds.<sup>62</sup> Using eq 3 we obtain the relatively low estimate of -6.7for the basicity of water, which agrees with the value of -6.66 reported by Deno and Taft in concentrated sulfuric acid.<sup>63</sup> The estimated  $pK_a$  values for ethanol (-5.1) and diethyl ether (-5.1) are in disagreement with the results of distribution studies but are very close to some of the Raman spectroscopy results for alcohols (see Table I). In view of the particular difficulty in defining the solvated free base and ionic species for water and the alcohols in aqueous strong acids, we think there is little profit in discussing agreement with these other estimates. As Table I shows, it would be remarkable if any number we obtained were not fortuitously close to some previously determined value.

This calorimetric basicity scale should be useful in evaluating the relative basicities of other important classes of compounds and for discriminating among widely varying estimates in aqueous acid. We have applied the treatment to the determination of the base strengths of carbonyl compounds and will report our results in the following paper.

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<sup>(55) (</sup>a) See ref 3, pp 147, 153, 210; (b) see ref 3, p 205.
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Soc., 83, 3819 (1961); (b) R. F. Brown, J. Org. Chem., 27, 3015 (1962).
(57) J. J. Christensen, J. L. Oscarson, and R. M. Izatt, J. Am. Chem. Soc., 90, 5949 (1968), and references cited therein.

<sup>(58)</sup> The ionization of anilinium ions in dilute aqueous acid is one reaction series which does apparently obey both of these relationships. See P. D. Bolton and F. M. Hall, J. Chem. Soc., B, 259 (1969), and A. I. Biggs and R. A. Robinson, ibid., 388 (1961).

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<sup>(60) (</sup>a) E. Grunwald and S. Winstein, J. Am. Chem. Soc., 70, 846 (1948); (b) A. H. Fainberg and S. Winstein, *ibid.*, 78, 2770 (1956); (c) J. Wilputte-Steinert and P. J. C. Fierens, *Bull. Soc. Chim. Belges*, 64, 308 (1955).

<sup>(61)</sup> D. D. Perrin, "Dissociation Constants of Organic Bases in Aqueous Solution," Butterworth and Co., Ltd., London, 1965.
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